## Year 1 Applied Chapter 5: Probability - Exam Questions (Total Marks 38)

Q1.


Figure 1

Figure 1 shows how 25 people travelled to work.
Their travel to work is represented by the events
$B$ bicycle
$T$ train
W walk
(a) Write down 2 of these events that are mutually exclusive. Give a reason for your answer.
(b) Determine whether or not $B$ and $T$ are independent events.

One person is chosen at random. Find the probability that this person
(c) walks to work,
(d) travels to work by bicycle and train.

Q2.In a factory, three machines, $J, K$ and $L$, are used to make biscuits.
Machine $J$ makes $25 \%$ of the biscuits.
Machine $K$ makes $45 \%$ of the biscuits.
The rest of the biscuits are made by machine $L$.
It is known that $2 \%$ of the biscuits made by machine $J$ are broken, $3 \%$ of the biscuits made by machine $K$ are broken and $5 \%$ of the biscuits made by machine $L$ are broken.
(a) Draw a tree diagram to illustrate all the possible outcomes and associated probabilities.

A biscuit is selected at random.
(b) Calculate the probability that the biscuit is made by machine $J$ and is not broken.
(c) Calculate the probability that the biscuit is broken.

Q3.The Venn diagram shows the probabilities of customer bookings at Harry's hotel.
$R$ is the event that a customer books a room
$B$ is the event that a customer books breakfast $D$ is the event that a customer books dinner $u$ and $t$ are probabilities.

(a) Write down the probability that a customer books breakfast but does not book a room.

Given that the events $B$ and $D$ are independent
(b) find the value of $t$
(c) hence find the value of $u$

Q4.
The events $A$ and $B$ are such that $\mathrm{P}(A)=\frac{1}{3}$ and $\mathrm{P}(B)=\frac{1}{4} \cdot \mathrm{P}(A$ or $B$ or both $)=\frac{1}{2}$.
a Represent these probabilities on a Venn diagram.
b Show that $A$ and $B$ are independent.

Q5.
For events $J$ and $K, \mathrm{P}(J$ or $K$ or both $)=0.5, \mathrm{P}(K$ but not $J)=0.2$ and $\mathrm{P}(J$ but not $K)=0.25$.
a Draw a Venn diagram to represent events $J$ and $K$ and the sample space $S$.
b Determine whether events $J$ and $K$ are independent.

## Q6.

In a factory, machines $A, B$ and $C$ produce electronic components. Machine $A$ produces $16 \%$ of the components, machine $B$ produces $50 \%$ of the components and machine $C$ produces the rest. Some of the components are defective. Machine $A$ produces $4 \%$, machine $B 3 \%$ and machine $C 7 \%$ defective components.
a Draw a tree diagram to represent this information.
b Find the probability that a randomly selected component is:
i produced by machine $B$ and is defective ii defective.

